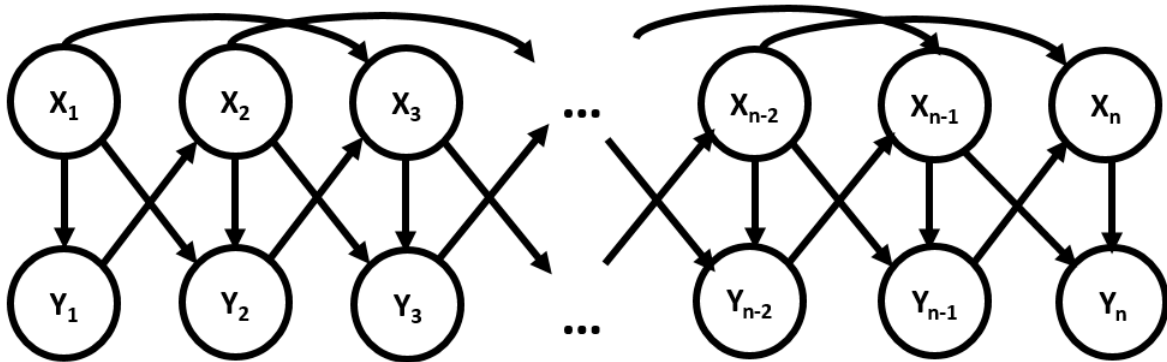


Homework 3

Q1- Variable Elimination

Consider the following Bayesian network.



A) Draw the corresponding Markov network.

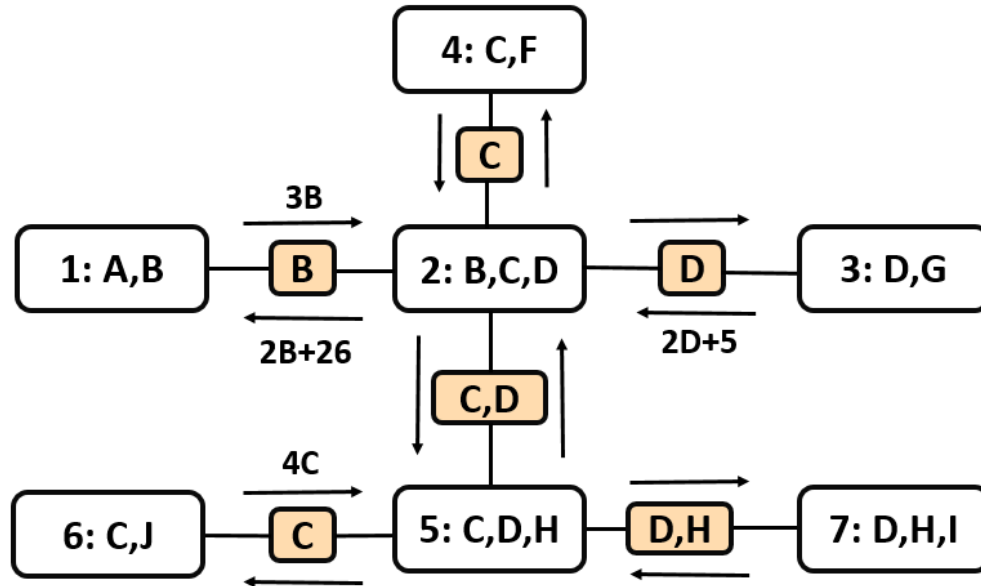
B) Now, apply the following variable elimination orders and draw the corresponding induced graph.

- 1) $Y_1, X_1, Y_2, X_2, \dots, Y_n, X_n$
- 2) $X_1, Y_1, X_2, Y_2, \dots, X_n, Y_n$

C) Given that X_i s and Y_i s are binary variables, which of the above variable elimination orders is optimal?

Q2- Junction tree

Consider the following junction tree for performing **max-sum message passing** on a Markov Random Field network.



A) Draw a Markov network corresponding to this junction tree.

B) Assume that all variables are binary and the potentials of clusters are as below.

$$\phi_1(A, B) = \exp(\alpha 1(A = B = 1)),$$

$$\phi_2(B, C, D) = \exp(2B + \gamma C + \lambda D),$$

$$\phi_3(D, G) = \exp(2D + \lambda G),$$

$$\phi_4(C, F) = \exp(1(C = F)),$$

$$\phi_5(C, D, H) = \exp(1(C = D) + DH),$$

$$\phi_6(C, J) = \exp(\zeta CJ),$$

$$\phi_7(D, H, I) = \exp(1(D = H = 1) + 1(H \neq I))$$

where $1(\cdot)$ is an indicator function.

Find the values of α , γ , λ and ζ . (Compute all necessary messages for finding these variables.)